Correlation of Photodetachment Rate and Lyapunov Exponent for a Scarred Resonance State

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Model & Previous Results

• Driven Inverted Gaussian (rad. gauge, atomic units)

$$H = \frac{1}{2} \left[p - \frac{\varepsilon}{\omega} \sin \omega t \right]^2 - V_0 \exp \left[- \left(\frac{x}{a} \right)^2 \right]$$

• $V_0 = 0.63$ a.u., a = 2.65 a.u., $\omega = 0.0925$ a.u., ε is varied

- Number of quantum resonance states increases as ε is increased (Ben-Tal, Moiseyev, and Kosloff, J. Chem. Phys. 98, 9610 (1993)).
- Light-induced resonance states are scarred on unstable periodic orbits of the classical motion (T. Timberlake and L. E. Reichl, Phys. Rev. A 64, 033404 (2001)).
- Possible connection between scarring and stabilization against ionization?

Classical Dynamics

- Four periodic orbits of period $T = 2\pi/\omega$.
- Orbit A is stable and surrounded by a stable island that decreases in size as ε is increased.
- Orbits B, C, and D are unstable and move apart along p = 0 as ε is increased.



Scarred Resonance State

- One of the light-induced resonance states that is created as ε is increased has Husimi distributions that are peaked on Orbit C.
- This state is a scar of Orbit C.



Quantum-Classical Correspondence

- The continuous line shows the Lyapunov exponent (λ) of Orbit C.
- The data points show the photodetachment rate (Γ) of the scarred state. Note that the lifetime is $\tau = 1/\Gamma$.
- Note the similar behavior as a function of ε .



Correlation of λ and Γ

- Strong correlation over all field strengths (R = 0.953).
- Best-fit line:
- $\Gamma = 1.505\lambda 0.010$ a.u.
- Very linear in restricted range with R = 0.993.
- Best-fit line:

 $\Gamma = 1.496\lambda - 0.013$ a.u.



Stable Island State

• The resonance state that is connected to the ground state as $\varepsilon \rightarrow 0$ remains peaked inside the stable island until ε becomes large.



Γ for Stable Island State

- The photodetachment rate (Γ) of the stable island state increases as ε increases (and the size of the classical stable island decreases).
- The jumps in the plot may be due to avoided crossings in the Floquet spectrum.



Conclusions

- The lifetime of the stable island state gets shorter and the lifetime of the scarred state gets longer as ε is increased.
- For large ε the scarred state is the longest-lived resonance and its lifetime continues to increase as ε is increased.
- This is evidence for quantum stabilization on an unstable classical structure, but this behavior is still correlated with a classical quantity: the Lyapunov exponent of the unstable orbit.
- The correlation between the photodetachment rate and the Lyapunov exponent represents a new type of quantum-classical correspondence.